

- Summary of solution

Mem.	Design load	$A_g$	$A_n$	U	$A_e$	Yield strength	Fracture strength	Block-shear strength
L4x3x1/2	100 kips	3.25	2.69	0.9	2.41	105 kips	104.8 kips	119.13 kips
		Design strength = 104.8 kips (net section fracture governs) L4x3x1/2 is adequate for $P_u = 100$ kips and the given connection						

- Note: For this problem  $A_e/A_g = 2.41/3.25 = 0.741$ , which is  $< 0.745$ . As predicted by the AISC manual, when  $A_e/A_g < 0.745$ , net section fracture governs.

20/10/15

## Design of compression members

- A vertical compression member in a building is called post (or) stanchion (or) column. compression member in a truss is strut.
- compression member in a crane is called boom.
- columns are classified into i) short ii) intermediate iii) long

when the loads are acting 100% concentric, then the column fails due to crushing of the material (or) yielding of the material in compression. Generally the short columns will fail due to crushing of the material.

All the times it is not possible to have 100% axial load. Hence small (or) large eccentricity will form and a column will buckle (bend) when subjected to this eccentric loading. Due to this buckling the material will fail before it reaches crushing value.  $\therefore$  the load carrying capacity for an eccentrically loaded column decreases.

Generally all the intermediate & long columns will buckle. As per IS 800 : 2007, the buckling is classified into four categories class a, class b, class c and class d.

theoretically the buckling is classified into

- 1) Local buckling - In this the individual elements of the column like flange (or) web buckle due to external loading. This can be prevented by providing suitable width to thickness ratio.
- 2) Flexural buckling (Euler's buckling) - Here the total column section buckles along its length. Generally the column bends about the axis corresponding to the largest slenderness ratio. Usually the minor principal axis will have least radius of gyration and hence buckles around that axis.

\* Compression members of all types of cross-section configuration will fail in this way.

- 3) Torsional buckling - Thin wall members with open c/s shape are sometimes weak in torsion and hence may buckle by twisting rather than buckling. Torsional buckling occurs when

$$\text{Torsional rigidity} < \text{Flexural rigidity}$$

(CJ)  $\text{EI}$   
 \* All standard hot rolled sections are not susceptible to



Built-up members with thin plates will sometimes subjected

Torsional buckling \*

4) Flexural-Torsional buckling - This type of failure occurs due to combination of flexural buckling & torsional buckling i.e. the member bends and twists simultaneously.

\* Unsymmetrical cross-sections with one axis of symmetry or no axis of symmetry are susceptible for such type of buckling.

\* clauses 7.1 (Section-7) / Page 34-44 \*

(Flexural buckling)

\* Calculate the design compressive load capacity of the column ISHB 300 @ 517 N/m if the length of the column is 3m.

i) If both ends are pinned ii) if column is restrained in direction and position at both ends.

Sol From steel tables, details of ISHB 300 @ 517 N/m

$$h = 300 \text{ mm}, b_f = 250 \text{ mm}, t_f = 10.6 \text{ mm}, A = 7484 \text{ mm}^2$$

$$\left( \frac{h}{b_f} = \frac{300}{250} = 1.2; t_f = 10.6 \text{ mm} \right) \quad \text{From Table-10, For I-section the}$$
$$\frac{h}{b_f} \leq 1.2 \quad \leq 100 \text{ mm}$$

column buckles about z-z axis with Buckling class-b

case

i) Given Length of the column (L) = 3m

$$\text{Effective length (KL)} = 1.0L \quad \left( \because \text{from Table-11} \right)$$

Both ends pinned (Hinged)

$$\text{i.e. (KL)} = 3000 \text{ mm}$$

@ column buckles about z-z axis with buckling class-b

$$\text{slenderness ratio } \left( \frac{KL}{r} \right) = \frac{KL}{r_{zz}} = \frac{3000}{129.5} = 23.17 \quad r_{zz} = 129.5 \text{ mm}$$
$$r_{yy} = 54.1 \text{ mm}$$

$$\text{As per cl 7.1.2.1, } f_{cc} = \text{Euler buckling stress} = \frac{\pi^2 E}{\left( \frac{KL}{r} \right)^2}$$

$$= \frac{\pi^2 \times 2 \times 10^5}{(23.17)^2}$$

$$\Rightarrow f_{cc} = 3678.13 \text{ N/mm}^2$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{3678.13}} \Rightarrow \lambda = 0.26$$

$$\phi = 0.5 [1 + \alpha(\lambda - 0.2) + \lambda^2]$$

$$= 0.5 [1 + 0.34(0.26 - 0.2) + 0.26^2]$$

$$\alpha = 0.34 \left( \frac{\text{table-7}}{35} \right) \text{ for class-b}$$

$$\Rightarrow \phi = 0.544$$

design compressive stress,  $f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} \left( = \frac{\chi f_y}{\gamma_{mo}} \leq \frac{f_y}{\gamma_{mo}} \right)$

$$\Rightarrow f_{cd} = \frac{250/1.1}{0.544 + [0.544^2 - 0.26^2]^{0.5}} = 282.41 \text{ N/mm}^2$$

$$\left( \chi = \frac{1}{[\phi + (\phi^2 - \lambda^2)^{0.5}]} \right)$$

$$= 0.9786$$

As per 7.1.2

$$P_d = A_e f_{cd}$$

$$\text{here } A_e = A_g$$

$$\left( \text{As per } \frac{7.3.2}{46} \right)$$

$$\Rightarrow P_d = A_g f_{cd}$$

$$= 7484 \times 282.41$$

$$\Rightarrow P_d = 1664.52 \text{ kN}$$

⑥ column buckles about y-y axis with buckling class-c

$$\text{slenderness ratio} = \frac{KL}{r_{yy}} = \frac{3000}{51.1} = 55.45$$

As per cl. 7.1.2

$$f_{cc} = \frac{\pi^2 E}{\left( \frac{KL}{r} \right)^2}$$

$$f_{cc} = 641.98 \text{ N/mm}^2$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{641.98}}$$

$$\Rightarrow \lambda = 0.624$$

$$\alpha = 0.49 \text{ for class-c } \left( \frac{\text{table-7}}{35} \right)$$

$$\phi = 0.5 [1 + \alpha(\lambda - 0.2) + \lambda^2] = 0.5 [1 + 0.49(0.624 - 0.2) + 0.624^2]$$

$$\Rightarrow \phi = 0.798$$

$$\text{Now, } f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} = \frac{250/1.1}{0.798 + [0.798^2 - 0.624^2]^{0.5}} \Rightarrow f_{cd} = 175.36 \text{ N/mm}^2$$

$$P_d = A_g f_{cd}$$

$$= 7484 \times 175.36$$

$\therefore$  Design Compressive strength capacity of column when both ends are pinned = 1312.43 kN

$$P_d = 1312.43 \text{ kN}$$



Case-(1) Restrained in direction & position at both ends

$$\text{Now effective length (KL)} = 0.65L \quad \left( \because \text{From Table-11} \right) \\ = 0.65 \times 3000$$

$$\Rightarrow \underline{KL = 1950 \text{ mm}}$$

(a) Column buckles about z-z axis with buckling class 'b'.

$$\text{Slenderness ratio} = \frac{KL}{r_{zz}} = \frac{1950}{129.5} = 15.05$$

By interpolation,

$\frac{KL}{r}$	$f_{cd}$
10	227
20	225

$$\text{for } \frac{KL}{r} \text{ at } 15.05, \quad f_{cd} = 227 - \frac{2}{10}(227 - 225) \\ f_{cd} = 226.6 \text{ N/mm}^2$$

$$P_d = A_g f_{cd} \\ = 7484 \times 226.6$$

$$P_d = 1695.874 \text{ kN}$$

(b) Column buckles about y-y axis with buckling class 'c'

$$\frac{KL}{r_{yy}} = \frac{1950}{54.1} = 36.04$$

$\frac{KL}{r}$	$f_{cd}$
30	211
40	198

$$f_{cd} \text{ at } \frac{KL}{r} = 36.04 = 211 - \frac{6.04}{10}(211 - 198) \\ = 203.148 \text{ N/mm}^2$$

$$P_d = A_g f_{cd}$$

$$= 7484 \times 203.148$$

$$P_d = 1520.35 \text{ kN}$$

Problem on Flexural torsional buckling

An ISA 100 100, 6 mm is used as a strut in a truss. Length of strut b/n intersections at each end is 3m. Calculate the strength of strut if (i) ends are fixed (ii) ends are hinged (iii) connected by two bolts at each end (iv) connected by 1 bolt at each end (v) connected by welding at each end

Sol For ISA 100 100, 6 mm,  $A = 1167 \text{ mm}^2$ ;  $r_{yy} = 19.5 \text{ mm}$  (steel tables)

(i) Ends are fixed

(i) connected by two bolts at each end. Given  $L = 3 \text{ m}$

As per 7.1.2/48,  $\lambda_e = \sqrt{K_1 + K_2 \lambda_{vv}^2 + K_3 \lambda_\phi^2}$

From table-12/48,  $K_1 = 0.20$  (for fixed and two bolts)  
 $K_2 = 0.35$   
 $K_3 = 20$

$\lambda_{vv} = \frac{\left(\frac{L}{r_{vv}}\right)}{\epsilon \sqrt{\frac{\pi^2 E}{250}}} = \frac{3000/19.5}{1 \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}}$ ;  $\epsilon = \left(\frac{250}{f_y}\right)^{0.5} = \left(\frac{250}{250}\right)^{0.5} = 1$

$\Rightarrow \lambda_{vv} = 1.73$

$\lambda_\phi = \frac{(b_1 + b_2)/2t}{\epsilon \sqrt{\frac{\pi^2 E}{250}}} = \frac{(100 + 100)/2 \times 6}{1 \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}} \Rightarrow \lambda_\phi = 0.187$

$\therefore \lambda_e = \sqrt{0.2 + (0.35 \times 1.73^2) + (20 \times 0.187^2)}$

$\Rightarrow \lambda_e = 1.395$

11/3/15 As per 7.1.2/34,  $\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2]$  ( $\lambda = \lambda_e$ )

$\alpha = 0.49$  (Table-7/35)  $\left( \because \text{L-section-class C - Table-10/44} \right)$

$\Rightarrow \phi = 0.5 [1 + 0.49 (1.395 - 0.2) + 1.395^2]$

$\Rightarrow \phi = 1.765$

$f_{cd} = \frac{f_y / r_{min}}{\phi + [\phi^2 - \lambda^2]^{0.5}} = \frac{250/1.1}{1.765 + [1.765^2 - 1.395^2]^{0.5}} \Rightarrow f_{cd} = 79.84 \text{ N/mm}^2$

Q. 7.1.2/34,  $P_d = A_e f_{cd}$   $A_e = A_g \left( \frac{1.73 \cdot 2}{4.6} \right)$

$P_d = 1167 \times 79.84 \Rightarrow P_d = 93.17 \text{ kN}$



c) i) connected by 1 bolt at each end

From Table - 12  
48  $K_1 = 0.75$  ;  $K_2 = 0.35$  ;  $K_3 = 20$

$$\lambda_e = \sqrt{K_1 + K_2 \lambda_{vv}^2 + K_3 \lambda_{\phi}^2}$$

$$= \sqrt{0.75 + (0.35 \times 1.73^2) + (20 \times 0.187^2)}$$

$$\Rightarrow \lambda_e = 1.58$$

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2] = 0.5 [1 + 0.49 (1.58 - 0.2) + 1.58^2]$$

$$\Rightarrow \phi = 2.086$$

$$f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} = \frac{250 / 1.1}{2.086 + [2.086^2 - 1.58^2]^{0.5}} \Rightarrow f_{cd} = 65.9 \text{ N/mm}^2$$

$$P_d = A_e f_{cd} = 1167 \times 65.9 = 76.9 \times 10^3 \text{ N}$$

$$\Rightarrow P_e = 76.9 \text{ kN}$$

ii) connected by welding at each end  
The strength of welded strut will be same as that of single angle The strength of welded strut will be same as that of single angle The strength of welded strut will be same as that of single angle  
Strut connected with two bolts at each end with the ends considered fixed.

⑥ Ends are hinged

i) connected by two bolts at each end

$$\lambda_e = \sqrt{K_1 + K_2 \lambda_{vv}^2 + K_3 \lambda_{\phi}^2}$$

From table - 12  
48

$$K_1 = 0.70$$

$$\lambda_{vv} = 1.73$$

$$K_2 = 0.60$$

$$\lambda_{\phi} = 0.187$$

$$K_3 = 5$$

$$\Rightarrow \lambda_e = \sqrt{0.7 + (0.6 \times 1.73^2) + (5 \times 0.187^2)}$$

$$\Rightarrow \lambda_e = 1.634$$

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2] = 0.5 [1 + 0.49 (1.634 - 0.2) + 1.634^2]$$

$$\Rightarrow \phi = 2.18$$

$$f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + [\phi^2 - \lambda^2]^{0.5}} \Rightarrow f_{cd} = 62.73 \text{ N/mm}^2$$

$$P_d = A_e f_{cd} = 1167 \times 62.73 = 73.2 \times 10^3 \text{ N}$$

$$\Rightarrow P_d = 73.2 \text{ kN}$$

ii) & iii) are calculated.

## \* Design of Compression Members:

Procedure:

Step-1: Assume design compressive stress ( $f_{cd}$ )

$$f_{cd} = 90 \text{ N/mm}^2 \quad \text{— For Angle struts having } \frac{KL}{r} = 110 \text{ to } 130$$

$$f_{cd} = 135 \text{ N/mm}^2 \quad \text{— For Beam Sections (I) } \frac{KL}{r} = 70 \text{ to } 90$$

$$f_{cd} = 200 \text{ N/mm}^2 \quad \text{— For Compression members carrying large loads}$$

Step-2: calculate ' $A_g$ ' using  $A_g = \frac{P_u}{f_{cd}}$  ;  $P_u$  = factored compressive load

Step-3: select a  $\Delta$  having area more than  $A_g$  required

calculate  $r_{min}$  ← Step-4:

Step-5: Determine Effective length based on end conditions

find slenderness ratio  $\left(\frac{KL}{r_{min}}\right)$  must be

Step-6: calculate  $P_d = A_g f_{cd} > P_u$

\* Design a single angle discontinuous strut to carry a factored axial compressive load of 65 kN. Length of strut is 3m b/n intersection. It is connected to a 12mm thick gusset plate by 20mm dia. 4.6 grade bolts. Use Fe410 steel.

Given data :  $P_u = 65 \text{ kN}$  ,  $L = 3 \text{ m}$  ,  $d = 20 \text{ mm}$

Assuming  $f_{cd} = 90 \text{ N/mm}^2$  for Angle strut  $d_h = 22 \text{ mm}$

$$A_{g \text{ required}} = \frac{P_u}{f_{cd}} \Rightarrow A_{g \text{ req}} = \frac{65 \times 10^3}{90}$$

$$= 722.22 \text{ mm}^2$$

Try ISA 70 10, 8 mm having  $A_g = 1058 \text{ mm}^2 (> 722.22 \text{ mm}^2)$

$$r_{yy} = 13.5 \text{ mm}$$

Calculation of no. of bolts required

Strength of 20mm dia. 4.6 grade bolts

$$\text{In single shear, } V_{dsb} = \frac{V_{nsb}}{r_{mb}}$$

$$\left( \frac{0.10 \cdot 3.3}{1.25} \right)$$

$$= \frac{f_u}{\sqrt{3}} (n_n A_{nb} + A_{sb} n_s) \frac{1}{r_{mb}}$$

$$= \frac{400}{\sqrt{3}} \left( 0 + 0.78 \cdot \frac{\pi \cdot 20^2}{4} \right) \frac{1}{1.25}$$

$$\Rightarrow V_{dsb} = 45.27 \text{ kN}$$



c) In bearing  $V_{dpb} = 2.5 k_b d t \frac{f_u}{r_{mb}}$

$$\left( \frac{d \cdot 10 \cdot 3 \cdot 4}{75} \right)$$

$$k_b = \frac{e}{3d_o}, \frac{p}{3d_o} = 0.25, \frac{f_{ub}}{f_u}, 1.0$$

$e \neq 1.5d_n \neq 1.5 \times 22 \neq 33$   
 $p \neq 2.5d_n \neq 2.5 \times 20 \neq 50$

$$= \frac{40}{3 \times 22}, \frac{50}{3 \times 22} = 0.25, \frac{400}{410}, 1.0$$

$$\left( \frac{40}{3 \times 22} \right) = 0.606, \left( \frac{50}{3 \times 22} \right) = 0.507, \left( \frac{400}{410} \right) = 0.975$$

$$\Rightarrow V_{dpb} = 2.5 \times 0.507 \times 20 \times 8 \times \frac{410}{1.25}$$

$$\Rightarrow V_{dpb} = 66.58 \text{ kN}$$

$\therefore$  strength of bolt is 45.27 kN

$$\text{No. of bolts required} = \frac{P_u}{V_{dsb}} = \frac{65}{45.27} = 1.4 \approx \underline{\underline{2 \text{ bolts}}}$$

Assume fixed hinged ends, from Table-12,  $k_1 = 0.20$   
 $k_2 = 0.60$   $0.35$   
 $k_3 = 2.0$

As per  $\frac{7.5 \cdot 1.2}{48}$ ,  $\lambda_e = \sqrt{k_1 + k_2 \lambda_w^2 + k_3 \lambda_\phi^2}$

$$\lambda_w = \frac{\left( \frac{l}{r_w} \right)}{\sqrt{\frac{\pi^2 E}{250}}} = \frac{(3000/35)}{\sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}} = 2.5$$

$$E = \left( \frac{f_y}{250} \right)^{0.5} = 1$$

$$\lambda_\phi = \frac{(b_1 + b_2)/2t}{\sqrt{\frac{\pi^2 E}{250}}} = \frac{(70 + 70)/2 \times 8}{\sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}} = 0.0984$$

$$\Rightarrow \lambda_e = \sqrt{(0.20) + (0.60 \times 2.5^2) + (2.0 \times 0.0984^2)}$$

$$\Rightarrow \lambda_e = 2 \times 1.606 \quad \text{Table-7/35} \quad (\alpha = 0.49 \text{ for class-C})$$

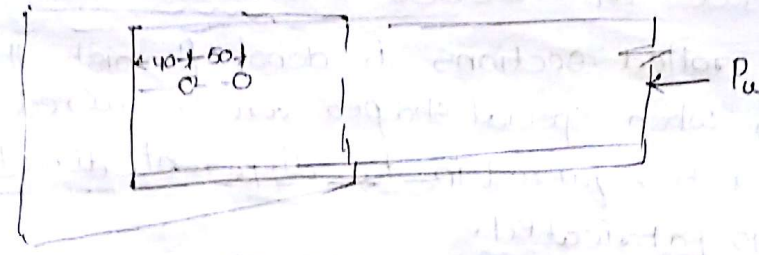
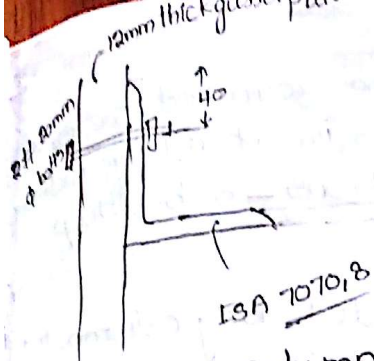
$$\phi = 0.5 \left[ 1 + \alpha (\lambda_e - 0.2) + \lambda_e^2 \right] = 0.5 \left[ 1 + 0.49 (1.606 - 0.2) + 1.606^2 \right]$$

$$\Rightarrow \phi = 3.2176$$

$$f_{cd} = \frac{f_y / r_{mo}}{\phi + [\phi^2 - \lambda_e^2]^{0.5}} = \frac{64.31}{1.606} \text{ N/mm}^2$$

$$P_u = A_e f_{cd} = A_g f_{cd} = 1058 \times \frac{64.31}{1.606} = 67.93 \text{ kN} (> 65 \text{ kN})$$

Hence safe



\* Design a column to support a factored load of 1050 kN. Column has an effective length of 7m w.r.to z-axis and 5m w.r.to y-axis. Use Fe410 steel.

Given  $P_u = 1050 \text{ kN}$

Assuming  $f_{cd} = 135 \text{ N/mm}^2$  - for I-section

$$A_{g \text{ required}} = \frac{P_u}{f_{cd}} = \frac{1050 \times 10^3}{135} \Rightarrow A_{g \text{ req}} = 7777.77 \text{ mm}^2$$

Try ISHB 350 @ 661.8 N/m having  $A_g = 8591 \text{ mm}^2$  ( $> 7777.77 \text{ mm}^2$ )  
 $I_{zz} = 19159.7 \times 10^4 \text{ mm}^4$ ;  $I_{yy} = 2451.4 \times 10^4 \text{ mm}^4$ ;  $h = 350 \text{ mm}$ ;  $b_f = 250 \text{ mm}$   
 $t_p = 11.6 \text{ mm}$ ;  $r_{yy} = 53.4 \text{ mm}$ ;  $r_{zz} = 149.3 \text{ mm}$

$$\frac{h}{b_f} = \frac{350}{250} = 1.4 > 1.2 \text{ and } t_p = 11.6 \text{ mm} < 40 \text{ mm}$$

From Table-10, the given column buckles about z-z axis with class (a)  
 y-y axis - " " (b)

i) Buckling about z-z axis with class-a:  
 Given, Effective Length (KL) = 7m about z-z axis  
 $r_{zz} = 149.3 \text{ mm}$

$$\text{Slenderness ratio} \left( \frac{KL}{r_{zz}} \right) = \frac{7000}{149.3} = 46.88$$

$$f_y = 250 \text{ N/mm}^2$$

$$\text{From Table-9(a)} \frac{40}{40}, f_{cd} = 207.4 \text{ N/mm}^2$$

$$P_d = \frac{A_g f_{cd}}{A_g} = 8591 \times 207.4 = 1781.77 \text{ kN} (> 1050 \text{ kN})$$

Hence safe

ii) Buckling about y-y axis with class-b:  
 KL = 5m about y-y axis;  $r_{yy} = 53.4 \text{ mm}$

$$\frac{KL}{r_{yy}} = \frac{5000}{53.4} = 93.63 \text{ and } f_y = 250 \text{ N/mm}^2$$

$$P_d = A_g f_{cd} = 8591 \times 128.2 = 1101.36 \text{ kN} (> 1050 \text{ kN})$$



## Built-up (Columns) Sections

When rolled sections (i) donot furnish the required section area (ii) when special shapes are required (iii) when large radius of gyration is required in two different directions - a built-up section is fabricated.

For economical design of a heavily loaded long column the least radius of gyration of column section is increased to the maximum. For this the rolled sections are kept away from the centroidal axis of the column and connected by some connecting systems - called Lattice systems. Commonly, Lattice systems are two types - [ Lacing, Batten

Primary function of Lacings (or) Battens is to hold and keep the main member of built up column in their relative position. Hence they are not carried as load carrying elements.

Flats and angle sections are normally used as Lacings. Generally Lacings are connected with single bolt at the end. Lacings are subjected to shear forces due to horizontal forces on the column.

Lacings are designed for compression members and checked for tension.

- Design of Laced columns:
  1. Design of the column (Built-up):
    - a) For built-up columns assume  $f_{cd} = 150 \text{ to } 190 \text{ N/mm}^2$
    - b) While calculating Effective Slenderness ratio take ' $r_{min}$ ' as the maximum value of  $r_{yy}$  and  $r_{zz}$
    - c) As per cl. 7.6.1.5, Increase the  $\left(\frac{KL}{r}\right)$  value by 5%.
    - d) For spacing of column elements equate  $I_{yy}$  to  $I_{zz}$  for a built-up column.

2. Design of Lacings:
  - a) Assume single or double Lacing
  - b) Assume inclination of Lacings as per  $\frac{7.6.4.1}{50}$
  - c) Find compressive force in each Lacing part as per  $\frac{7.6.6.1}{50}$
  - d) Check  $\frac{\sigma_1}{\tau_1}$  as per  $\frac{7.6.5.1}{50}$

Find dimensions of Lacing part as per 7.6.2 and 7.6.3



- Find slenderness ratio,  $f_{cd}$  and  $P_d$  for Lacing bar
- check the lacing bar for tension as per  $\frac{6.2 \& 6.3}{32}$ .
- Design the connection of Lacing bar with main column
- Design the tie bar at the end as per  $\frac{7.7.2.2 \text{ and } 7.7.2.3}{51}$

Design a built-up column 10m long to carry a factored axial load of 1080 kN. column is restrained in position but not in direction at both ends. provide single lacing system with bolted connection.

Design the column with two channels placed back to back toe to toe

Design of built-up column:  
Assuming  $f_{cd} = 150 \text{ N/mm}^2$  for built-up column

Given  $P_u = 1080 \text{ kN}$

$$A_g \text{ required} = \frac{P_u}{f_{cd}} = \frac{1080 \times 10^3}{150}$$

$$\Rightarrow A_{g \text{ req}} = 7200 \text{ mm}^2$$

Try two ISMC 300 @ 351.2 N/m having  $A_g = 2 \times 4564 = 9128 \text{ mm}^2$  ( $> 7200 \text{ mm}^2$ )

From steel tables details of ISMC 300,  
 $A = 4564 \text{ mm}^2$ ;  $r_{yy} = 26.1 \text{ mm}$ ;  $r_{zz} = 118.1 \text{ mm}$ ;  $C_{yy} = 23.6 \text{ mm}$   
 $I_{zz} = 6368.6 \times 10^4 \text{ mm}^4$ ;  $I_{yy} = 310.8 \times 10^4 \text{ mm}^4$ ;  $b_f = 90 \text{ mm}$ ;  $t_f$

In the design of built-up columns with two sections the sections are so spaced that the least radius of gyration of the built-up section becomes as large as possible. This can be achieved by spacing the section in such a way that ' $r_{\min}$ ' is max. value of

$$r_{yy} \text{ (or) } r_{zz} \therefore r_{\min} = r_{zz} = 118.1 \text{ mm}$$

$$\frac{KL}{r_{\min}} = \frac{10 \times 10^3}{118.1} = 84.67 = \left( \frac{KL}{r} \right)_0$$

Effective length of column }  $KL = 1.0L$  (Table-1/45)

As per  $\frac{7.6.1.5}{48}$ ,  $\left( \frac{KL}{r} \right)_c = 1.05 \left( \frac{KL}{r} \right)_0$

$$\Rightarrow \left( \frac{KL}{r} \right)_c = 1.05 \times 84.67 = 88.9$$

$f_y = 250 \text{ N/mm}^2$

From Table-10, channel sections - Buckling class-C

From Table-9(C),  $f_{cd} = 122.65 \text{ N/mm}^2$



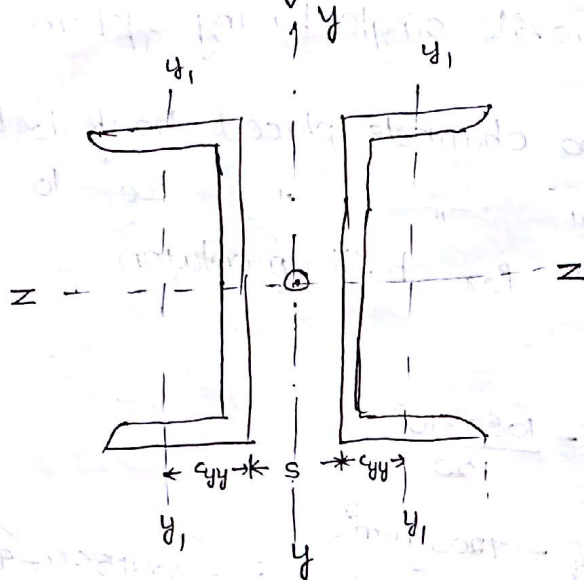
$$\Rightarrow P_d = A_e f_{cd} = (2 \times 4564) \times 122.65$$

$$\Rightarrow P_d = 1119.55 \text{ kN} (> 1080 \text{ kN})$$

Hence safe

@ Two channels placed back to back:

calculation of spacing of channels:



$$c_{yy} = 23.6 \text{ mm}$$

Let 's' be spacing of channels. z-z and y-y axes are centroidal axis for built-up section. y1-y1 is centroidal axis for individual channel section.

For calculation of 's' (for built-up section)  $I_{zz}$  is equated to  $I_{yy}$

$$\text{i.e. } I_{zz} = I_{yy}$$

$$2 \times 6362.6 \times 10^4 = [I_{yy} + ah^2] \times 2$$

$$= 2 \left[ 310.8 \times 10^4 + 4564 \times \left( \frac{s}{2} + 23.6 \right)^2 \right]$$

$$6362.6 \times 10^4 = \left[ 310.8 \times 10^4 + \left( \frac{s^2}{4} + 556.96 + 2 \left( \frac{s}{2} \times 23.6 \right) \right) 4564 \right]$$

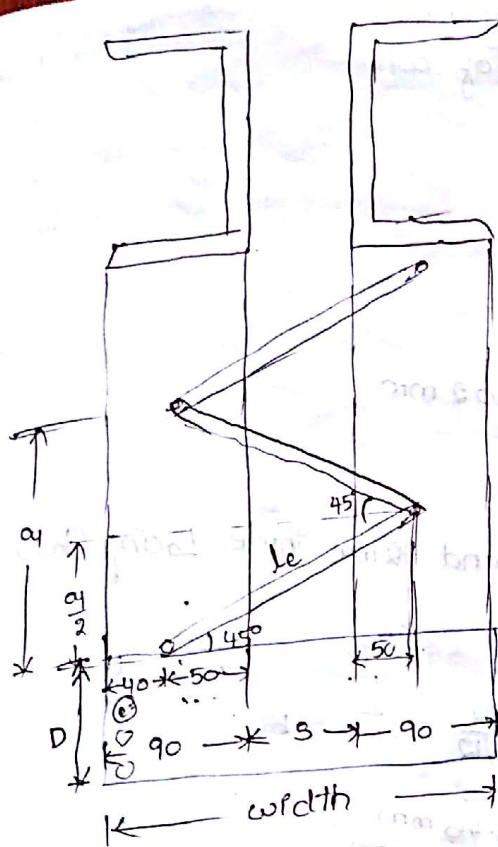
$$\Rightarrow (s^2 + 2227.84 + 94.49) 4564 = 6051.8 \times 10^4$$

$$\Rightarrow s = 183.1 \text{ mm} \text{ Say } 183.5 \text{ mm}$$

@ Lacing system:

Providing single Lacing system.

@ As per 7.6.4, Lacing bars can be inclined at  $40^\circ$  to  $70^\circ$  with horizontal. Hence provide single Lacing system at inclination of  $45^\circ$



$$\frac{180}{\sqrt{2}}$$

$$\frac{180}{\sqrt{2}} = \frac{180}{1.414} = 127.3$$

$$\frac{183.5}{\sqrt{2}} = \frac{183.5}{1.414} = 130.5$$

$$\tan 45^\circ = \frac{(a_1/2)}{183.5 + 50 + 50}$$

$$\Rightarrow a_1 = 567 \text{ mm}$$

Let  $l_e$  be effective length of lacing  $l_e = \sqrt{283.5^2 + 283.5^2}$   
 $\Rightarrow l_e = 400.93 \text{ mm}$

As per 7.6.5.1,  $r_1 = \text{min. radius of gyration of individual member}$   
 $\Rightarrow r_1 = 26.1 \text{ mm}$

$$\frac{a_1}{r_1} = \frac{567}{26.1} = 21.72 < 50 \quad \text{or} \quad 0.7 \left( \frac{KL}{r} \right)_e \quad \text{whichever is less}$$

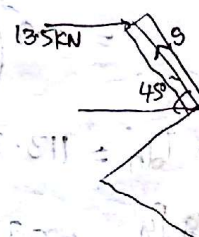
Hence OK  
 Design of Lacing bar:

As per 7.6.6.1, Total transverse shear = 8.5% of the axial force  
 $(V_L) = \frac{2.5}{100} \times 1080 = 27 \text{ kN}$

$V_L$  shall be divided equally among all transverse-lacing systems in parallel planes.

Transverse shear in each panel =  $\frac{27}{2} = 13.5 \text{ kN}$

Lacing is subjected to a compressive force of 19.09 kN. Hence the lacing is to be designed for this compressive load and should be checked for tension.



$$S \cos 45^\circ = 13.5$$

$$\Rightarrow S = 19.09 \text{ kN}$$

Size of Lacing as per 7.6.3, Assuming 16 mm dia. bolts for it



connection of Lacing with the main member.

width of Lacing =  $3 \times \text{Nominal dia. of bolt}$

$$= 3 \times 16$$

$$= 48 \text{ mm}$$

$$\text{say width} = 50 \text{ mm}$$

$$\text{thickness (t)} \neq \frac{1}{40} \times l_e$$

$$\neq \frac{1}{40} \times 400.93 \neq 10.02 \text{ mm}$$

provide 12 mm thick lacing

$\therefore$  Size of Lacing is 50 mm wide and 12 mm thick Lacing flats i.e.

50 ISF 12

$$r_{\min} = \sqrt{\frac{I_p}{A}} = \sqrt{\frac{\frac{bt^3}{12}}{bt}} = \frac{t}{\sqrt{12}} = \frac{12}{\sqrt{12}}$$

$$\Rightarrow r_{\min} = 3.46 \text{ mm}$$

$$\text{slenderness ratio } (\lambda) = \frac{l_e}{r_{\min}} = \frac{400.93}{3.46} = 115.74$$

Table-10  $\frac{44}{44}$ , Flat is under class-c buckling

from Table-9(c)  $\frac{42}{42}$ ,  $f_{cd} = 88.2 \text{ N/mm}^2$

$$P_d = A_g \times f_{cd} = (50 \times 12) 88.2 = 52.92 \times 10^3 \text{ N}$$

$$\Rightarrow P_d = 52.92 \text{ kN} > 19.09 \text{ kN}$$

Hence safe

check for tension for Lacing flats: d. 6.3 and 6.3

$$\textcircled{a} T_{dg} = \frac{A_g \times f_y}{\gamma_{mo}} = \frac{(50 \times 12)(250)}{1.1} \Rightarrow T_{dg} = 136.36 \text{ kN} (> 19.09 \text{ kN})$$

$$\textcircled{b} T_{dn} \text{ for plate} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

$$A_n = (50 - 18) 12$$

$$= 384 \text{ mm}^2$$

$$= 0.9 \left( \frac{384 \times 410}{1.25} \right)$$

$$\Rightarrow T_{dn} = 113.36 \text{ kN} (< 19.09 \text{ kN})$$

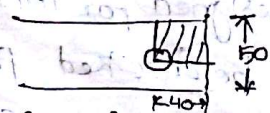
$$\textcircled{c} T_{db} = \left( \frac{A_{vg} f_y}{\gamma_{mo}} + 0.9 \frac{A_{tn} f_u}{\gamma_{m1}} \right) \textcircled{a}$$

$$A_{vg} = 40 \times 12 = 480 \text{ mm}^2$$

$$A_{vn} = (40 - \frac{1}{2} \times 18) 12 = 312 \text{ mm}^2$$

$$A_{tg} = (25 \times 12) = 300 \text{ mm}^2$$

$$A_{tn} = (25 - \frac{1}{2} \times 18) 12 = 192 \text{ mm}^2$$



$$T_{db} = \left( 0.9 A_m \frac{f_u}{\sqrt{3} f_m} + A_t g \frac{f_y}{f_m} \right) = 131.5 \text{ kN} > 19.09 \text{ kN}$$

Hence safe

$$(T_d > 19.09 \text{ kN})$$

connection with 16 mm dia. bolt to the main column

strength of 16 mm dia. bolt

i) In double shear,

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} f_{mb}} [n_n A_{nb} + n_s A_{sb}]$$

$$= \frac{400}{\sqrt{3} \times 1.25} \left[ \frac{\pi}{4} \times 16^2 + 0.78 \times \frac{\pi}{4} \times 16^2 \right]$$

ii) In bearing,

$$\Rightarrow V_{dsb} = 66.12 \text{ kN}$$

$$V_{dpsb} = 2.5 k_b d t \frac{f_u}{f_{mb}}$$

$$k_b = \frac{e}{3d_0}, \frac{p}{3d_0} - 0.25, \frac{f_{ub}}{f_u}, 1.0$$

$$e \nless 1.5 \times 18 + 27 \text{ mm}$$

$$p \nless 2.5 \times 16 + 40 \text{ mm}$$

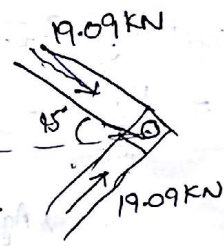
$$= 2.5 \times 0.491 \times 16 \times 12 \times \frac{410}{1.25} \left( \text{see } \frac{d_{10.3.4}}{15} \right)$$

$$\Rightarrow V_{dpsb} = 77.303 \text{ kN}$$

$\therefore$  strength of the bolt = 66.12 kN

SF coming on the bolt from the two lacing flats as shown

$$SF = 2 \times 19.09 \cos 45^\circ = 27 \text{ kN}$$



$$\therefore \text{No. of bolts required} = \frac{27}{66.12} = 0.408 \text{ say } \underline{1 \text{ bolt}}$$

connect 50 ISF 13 with 16 mm dia. bolt to the main column.

Design of Tie members

as per cl. 7.7.2.3, Tie plates are provided at the ends of Laced Columns

Effective depth  $\nless$  distance b/n centroids of main members

$$\text{width} = 183.5 + 90 + 90 = 363.5 \text{ mm}$$

$$\nless 5 + (2 \times 23.6)$$

$$\nless 230.7 \text{ mm} \nless 2 \times \text{width of 1 member} = 2 \times 90 = 180 \text{ mm}$$

$$\text{overall depth} = 230.7 + (2 \times e) = 230.7 + (2 \times 30) = 290.7 \approx 300 \text{ mm}$$

Thickness (t)  $\nless \frac{1}{50} \times$  Distance b/n innermost connecting lines of bolts  $\nless$  to main member

$$\nless \frac{1}{50} \times (183.5 + 50 + 50) \nless 5.6 \text{ mm}$$

$$\Rightarrow t = 6 \text{ mm}$$

Provide Tie plate of width 363.5 mm, 300 mm overall depth and 6 mm



2/3/15 (b) Two channels placed toe to toe:

spacing of channels (s):

$$I_{yy} = I_{zz}$$

$$2(I_{yy} + ah^2) = 2 I_{zz}$$

$$2 \left[ 310.8 \times 10^4 + (4564) \left( \frac{s}{2} - 23.6 \right)^2 \right] = 2 \times 6362.6 \times 10^4$$

$$\Rightarrow s = 277.5 \text{ mm}$$

Lacing system same as (a)

\* Design a built-up column with four angles. The column is 12m long and supports a factored axial compressive load of 700 kN. The ends of the column are held in position and restrained against rotation & Design a double Lacing system use Fe410 steel.

Sol Given data,  $P_u = 700 \text{ kN}$

Assuming  $f_{cd} = 170 \text{ N/mm}^2$

$$A_g \text{ required} = \frac{P_u}{f_{cd}} = \frac{700 \times 10^3}{170}$$

$$\Rightarrow A_{g \text{ req}} = 4117.65 \text{ mm}^2$$

Try ISA 90.90, 6 mm 4 numbers each

$$\text{area } A_g = 1047 \text{ mm}^2 ; c_{yy} = c_{zz} = 24.2 \text{ mm}$$

$$r_{yy} = r_{zz} = 27.7 \text{ mm} ; I_{yy} = I_{zz} = 80.1 \times 10^4 \text{ mm}^4$$

$$\text{Area of 4 angle sections} = 4 \times 1047 = 4188 \text{ mm}^2 (> 4117.65 \text{ mm}^2)$$

Arrangement of the angles:

Length of column (L) = 12m

$$\text{From Table -11, } KL = 0.65L = 0.65 \times 12 \times 10^3 = 7800 \text{ mm}$$

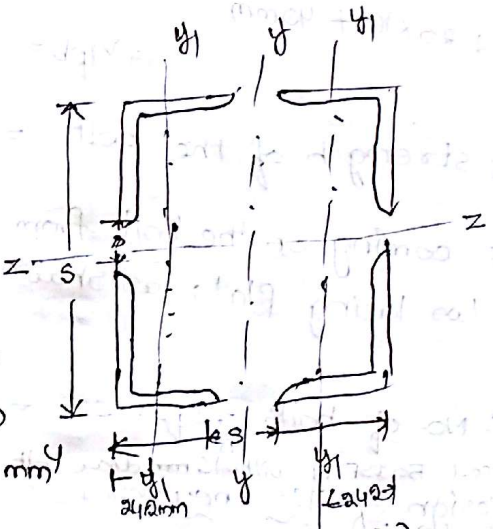
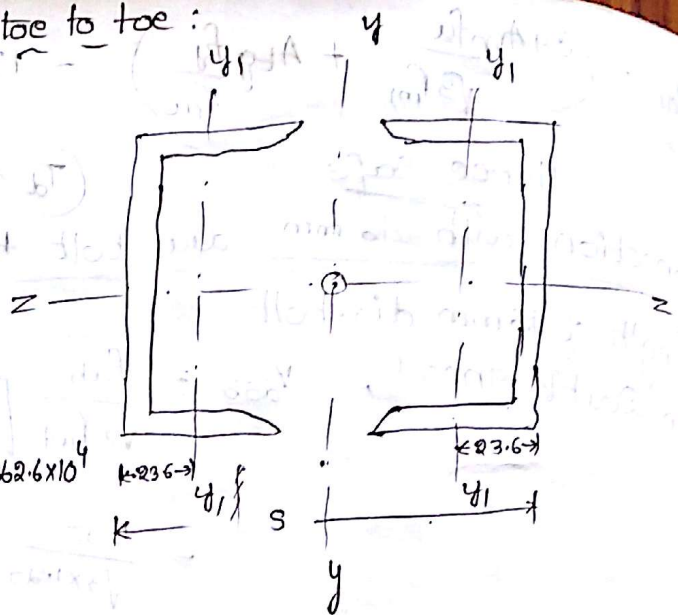
we have  $f_y = 250 \text{ N/mm}^2$  and  $f_{cd} = 170 \text{ N/mm}^2$

For Angle section, buckling class is C ( $\therefore$  From Table -10/44)

From page 42 - Table - 9(c)

$$\frac{KL}{r} = 58.67$$

$$\text{As per } \frac{7.6 \cdot 1.5}{48}, \left( \frac{KL}{r} \right)_0 = 1.05 \left( \frac{KL}{r} \right) = 1.05 \times 58.67$$



$$\Rightarrow r = \frac{7800}{61.6}$$

$$\Rightarrow r = 126.6 \text{ mm}$$

we know that  $I = AK^2 = Ar^2$

$$I = 4188 \times 126.6^2$$

$$\Rightarrow I_{\text{req}} = 6712.3 \times 10^4 \text{ mm}^4$$

Arranging 4 angle sections as shown. Let  $s$  be the spacing  
b/w the channels as shown.

$$I_{yy} = I_{zz} = I_{\text{required}}$$

$$4(I_{yy1} + ah^2) = I_{\text{required}}$$

$$\Rightarrow 4(80.1 \times 10^4 + 1047 \times (\frac{s}{2} - 24.2)^2) = 6712.3 \times 10^4$$

$$\Rightarrow s = 295.48 \text{ mm}$$

$$\text{ie } s = 295.5 \text{ mm}$$

As  $I_{yy} = I_{zz}$  for the builtup section, for the angle section  $I_{yy} = I_{zz}$

$\therefore$  the spacing of the builtup column in other direction, is also  $s = 295.5 \text{ mm}$

Hence the builtup column is a square column.

For  $(\frac{KL}{r})_e = 61.6$ ,  $f_y = 250 \text{ N/mm}^2$  and class-c buckling

as per Table-9C,  $f_{cd} = 165.44 \text{ N/mm}^2$

$$\therefore P_d = A_e f_{cd} = (4 \times 1047)(165.44) = 692.8 \text{ kN} (< 700 \text{ kN})$$

Hence Unsafe

Increase the spacing to 300 mm with 300 mm spacing  $I_{\text{provided}}$

$$\text{is } 4 \left[ 80.1 \times 10^4 + 1047 \left( \frac{300}{2} - 24.2 \right)^2 \right] = 6948.17 \times 10^4 \text{ mm}^4$$

$$I = Ar^2 \Rightarrow r = \frac{6948.17 \times 10^4}{4188} = 128.8 \text{ mm}$$

$$\left( \frac{KL}{r} \right)_e = \frac{7800}{128.8} = 60.5$$

From Table-9C,  $f_{cd} = 167.5 \text{ N/mm}^2$

$$\therefore P_d = (4 \times 1047)(167.5) = 701.5 \text{ kN} (> 700 \text{ kN})$$

Hence Safe

Double Lacing System!

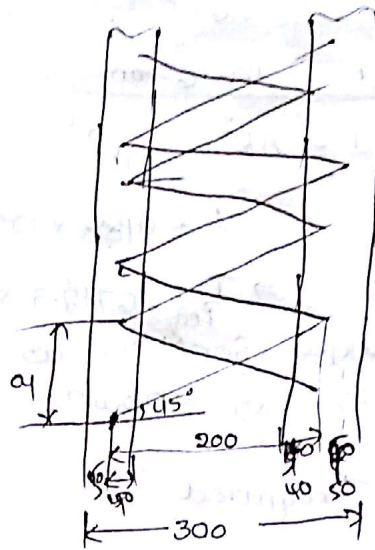
let the lacing flats be inclined at  $45^\circ$   $\left( \because \frac{7.64}{50} \right)$





$$\tan 45^\circ = \frac{a/2}{200} \Rightarrow a = 400 \text{ mm}$$

$$l = \frac{200}{\cos 45^\circ} \Rightarrow l = 282.84 \text{ mm}$$



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$$\left(\frac{a_1}{r_1}\right) = \frac{400}{27.7} = 14.44 < 50$$

$$\text{or } 0.7 \left(\frac{KL}{r}\right)_e$$

$$0.7 \times 60.5$$

$$= 42.35$$

Hence OK

$r_1$  = min. radius of gyration for individual member

$$= 27.7 \text{ mm} \left( \frac{0.7 \times 6.5 \times 50}{50} \right)$$

Design of Lacing bar

As per 7.6.6.1, Transverse shear ( $V_L$ ) = 2.5% of Axial force

$$= \frac{2.5}{100} \times 700$$

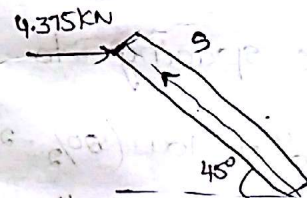
$$\Rightarrow V_L = 17.5 \text{ kN}$$

Force transferred in each lacing system =  $\frac{17.5}{2} = 8.75 \text{ kN}$

For double lacing system each lacing flat will be subjected to

$$\frac{8.75}{2} = 4.375 \text{ kN load (transverse)}$$

compressive force on the lacing bar



$$S \cos 45^\circ = 4.375$$

$$\Rightarrow S = 6.187 \text{ kN}$$

Lacing flat Design:

Each lacing flat should be designed for a compressive force of 6.187 kN and should be checked for tension.

Effective length of lacing bar is  $l_e$

$$\text{As per 7.6.3, } t \geq \frac{1}{60} \times l_e \quad \left[ \text{as per 7.6.6.3, } l_e = 0.7l \right]$$

$$= 0.7 \times 282.84$$

$$t \geq \frac{1}{60} \times 197.98$$

$$\Rightarrow l_e = 197.98 \text{ mm}$$

$$t \geq 3.299 \text{ say } 3.3 \text{ mm}$$

As per 7.6.3, minimum width = 3 dia. of bolt (Assume 16mm dia. bolt)

$$= 3 \times 16$$

$$= 48 \text{ mm}$$

$$\text{say } 50 \text{ mm}$$

provide 50 ISF 6

$$r_{min} \text{ for the flat} = \sqrt{\frac{I}{A}} = \sqrt{\frac{\frac{bt^3}{12}}{bt}} = \frac{t}{\sqrt{12}} = \frac{6}{\sqrt{12}}$$

$$\Rightarrow r_{min} = 1.732 \text{ mm}$$

Q1)  $\frac{le}{r} = \frac{197.98}{1.732} = 114.3$

for slenderness ratio - 114.3,  $f_y = 250 \text{ N/mm}^2$  and class-C

buckling from Table-9(c),  $f_{cd} = 89.7 \text{ N/mm}^2$

$$P_d = A_e \times f_{cd} = A_g \times f_{cd} = (50 \times 6) \times 89.7 = 26.91 \text{ kN} > 6.187 \text{ kN}$$

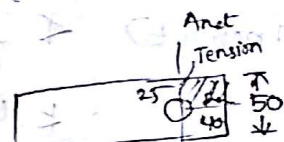
Hence Safe

Q2) check for stresses in Tension:

a)  $T_{dg} = \frac{A_g f_y}{\gamma_{mo}} = \frac{(50 \times 6)(250)}{1.1} = 68.18 \text{ kN} > 6.187 \text{ kN}$

b)  $T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}} = \frac{0.9 \times (50 - 18) \times 6 \times 410}{1.25}$

$\Rightarrow T_{dn} = 56.67 \text{ kN} > 6.187 \text{ kN}$



c)  $T_{db} = \frac{A_{vg} f_y}{\sqrt{3} \gamma_{mo}} + \frac{0.9 A_{tn} f_u}{\gamma_{m1}}$  (a)  $\frac{0.9 A_{tn} f_u}{\sqrt{3} \gamma_{m1}} + \frac{A_{tg} f_y}{\gamma_{mo}}$

59.83 kN (a)

$A_{vg} = 40 \times 6$

$A_{tg} = 25 \times 6$

$A_{vn} = (40 - \frac{1}{2} \times 18) \times 6$

$A_{tn} = (25 - \frac{1}{2} \times 18) \times 6$

Hence safe in compression as well as in Tension.

Connections:

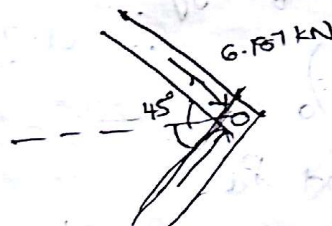
05/3/15

Q3) Force transmitted from

Q4)

the lacing bars on to the bolt =  $6.18 \cos 45^\circ \times 2$

= 8.74 kN



Using 16mm  $\phi$  bolts, strength of bolt in

@ Double shear  $(V_{dsb}) = \frac{f_u}{\sqrt{3} \gamma_{mb}} (n_p A_{nb} + n_s A_{sb})$

=  $\frac{410}{\sqrt{3} \times 1.25} \left[ 1 \times \frac{\pi}{4} \times 16^2 + 1 \times 0.78 \times \frac{\pi}{4} \times 16^2 \right]$

Q5)

Q6)

Bearing  $(V_{dpb}) = \frac{V_{dsb}}{2} = \frac{68.18 \text{ kN}}{2}$

=  $8.5 (k_b) d t \frac{f_u}{\gamma_{mb}} = 8.5 \times 0.49 \times 16 \times 6 \times \frac{410}{1.25}$

Q7)



$\therefore$  strength of bolt = 38.5 kN

no. of bolts required =  $\frac{8.75}{38.5} = 0.227 \approx 1$  bolt

tie plate

as per cl. 7.7.2.2, width = 300 mm

Eff. depth =  $d$  distance b/n centroids of main members

$d = 300 - (2 \times 24.2)$

$\Rightarrow d = 251.6$  mm

Overall depth =  $d + (2 \times e)$

$= 251 + (2 \times 40)$

$= 331$  mm say 340 mm

thickness (t)  $\geq \frac{1}{50} (300 - (2 \times 50))$

$\geq 4$  mm

say 6 mm thickness

Provide 340 mm overall depth and 6 mm thick tie plate one at the top end and another at the bottom end.

\* Design of column with Battens:

① Design of built-up column

② for built-up column assume  $f_{cd} = 150$  to  $190$  N/mm<sup>2</sup>

③ Take  $r_{min}$  as max. of  $r_{yy}$  and  $r_{zz}$ .

Find  $\left(\frac{KL}{r}\right)_e = 1.1 \left(\frac{KL}{r}\right)_0 \therefore \left(\frac{KL}{r}\right)_e = \frac{1.1 \times 7.7 \times 1.4}{51}$

④ calculate  $f_{cd}$  and  $P_d$

⑤ spacing of elements in the column

Equate  $I_{yy}$  to  $I_{zz}$  and increase the spacing to increase  $I_{yy}$

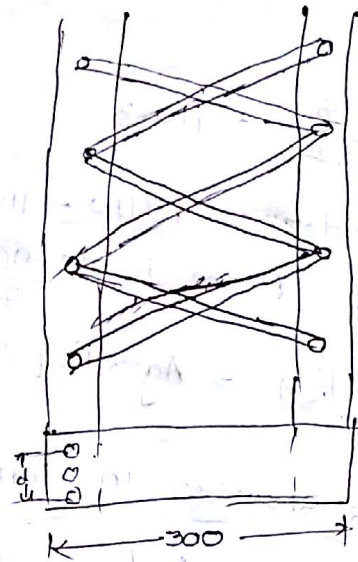
⑥ Design of Battens:  $\left(\frac{1.1 \times 7.7 \times 1.4}{50}\right)$

⑦ spacing of battens

⑧ size of end and intermediate battens.

⑨ Design forces on battens

⑩ check for shear stress and bending stresses for end battens and intermediate battens.



connections - should be designed to transmit both shear and bending moment.

② No. of batten plates

③ Real spacing of battens.

\* Design a built-up column 9m long to carry a factored axial compressive load of 1100 kN. Column is restrained in position but not in direction at both ends. Design the column with connecting systems as battens.

Use two channels back-to-back.

Sol Given data,  $P_u = 1100 \text{ kN}$  Design of built-up column

$$L = 9 \text{ m}$$

$$\text{Effective length (KL)} = 1.0L = 9 \text{ m}$$

( $\therefore$  from Table-11/45)

$$\text{Assume } f_{cd} = 150 \text{ N/mm}^2$$

$$A_{g \text{ required}} = \frac{P_u}{f_{cd}} = \frac{1100 \times 10^3}{150} = 7333.33 \text{ mm}^2$$

$$\text{Try 2 ISMC 200 @ } 351.2 \text{ N/m having } A_g = 2 \times 4564 = 9128 \text{ mm}^2 (> 7333.33 \text{ mm}^2)$$

Details

$$r_{zz} = 118.1 \text{ mm}$$

$$r_{yy} = 261 \text{ mm}$$

$$I_{zz} = 6366 \times 10^4 \text{ mm}^4$$

$$I_{yy} = 310.8 \times 10^4 \text{ mm}^4$$

$$c_{yy} = 23.6 \text{ mm}$$

$$b_f = 90 \text{ mm}$$

$$\text{Slenderness ratio } \left( \frac{KL}{r_{min}} \right) = \frac{9 \times 10^3}{118.1} = 76.2$$

$$\text{As per } \frac{7.71 \times 4}{51}, \left( \frac{KL}{r} \right)_e = 1.1 \left( \frac{KL}{r} \right)_0 = 1.1 \times 76.2 = 83.8$$

$$\text{Val For } \frac{KL}{r} = 83.8, f_{ty} = 250 \text{ N/mm}^2 \text{ For channel class-C (buckling Table-10/44)}$$

$$\text{From Table-9(C) } f_{cd} = 130.3 \text{ N/mm}^2$$

$$P_d = A_e f_{cd} = A_g f_{cd} = (2 \times 4564) 130.3 \Rightarrow P_d = 1189 \text{ kN} (> 1100 \text{ kN})$$

Hence safe

Arrangement and Spacing of channels:

Providing channels back to back to get the spacing b/n the channels Equate  $I_{yy}$  to  $I_{zz}$ .

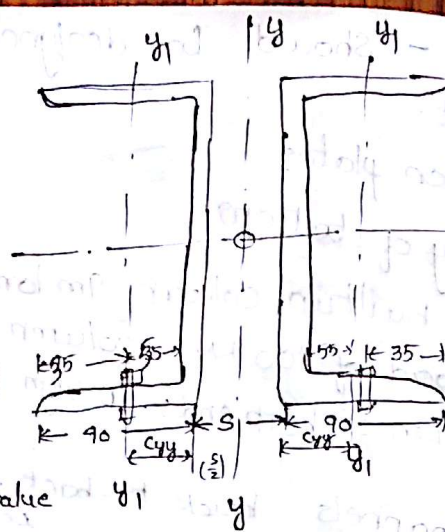


$$I_{yy} = I_{zz}$$

$$2[I_{yy} + ah^2] = 2 \times I_{zz}$$

$$\Rightarrow 2[310.8 \times 10^4 + (4564 \times (\frac{S}{2} + 236)^2)] = 2 \times 6366 \times 10^4$$

$$\Rightarrow S = 183.1 \text{ mm}$$



To make  $I_{yy} > I_{zz}$  increase S value

$$\text{Take } S = 200 \text{ mm}$$

Battens: (see cl. 7.7.1.3/50)

Battens or plates provided at top end of column, other at bottom end of column & others uniformly at equal spacing.

$$\text{Minimum no of battens} = 2 + 1 = 3$$

Spacing of Battens:

$$\frac{C}{r_y} < 0.1 \times \text{Slenderness ratio of column as a whole}$$

$$< 0.1 \times 83.82$$

$$< 58.67$$

$$C < 58.67 \times 261 < 1531.4 \text{ mm}$$

$$\frac{C}{r_y} \neq 50 \Rightarrow C \neq 1305 \text{ mm (see page - 51)}$$

provide battens at a spacing of 1300 mm

size of End battens:

Using flats for battens, using 20mm dia bolts for connection

$$d = 20 \text{ mm}$$

$$d_h = 22 \text{ mm}$$

$$e \leq 1.5 d_h \leq 1.5 \times 22 \leq 33 \text{ mm Say } 35 \text{ mm}$$

As per 7.7.2.3,  $d \leq$  distance b/n centroids of main members

$$d \leq 200 + (2 \times 236)$$

$$d \leq 247.2 \text{ mm}$$

$$\text{Overall Depth} = d + 2e$$

$$= 247.2 + 2 \times 35$$

$$= 317.2 \text{ mm Say } 320 \text{ mm}$$

$$\text{width of batten} = 200 + 90 + 90 = 380 \text{ mm}$$

$$\text{thickness } (t) \leq \frac{1}{50} \times (55 + 200 + 55) \leq 6.2 \text{ mm Say } 8 \text{ mm}$$

Hence provide 380 mm width, 320 mm overall depth and 8 mm thick end batten plate one at the top end and other at the bottom end of the column.

Use of Intermediate battens:  
 as per 7.7.3,  $d \leq \frac{3}{4} \sqrt{2500 (275.34)}$   
 $\Rightarrow d \leq 185.4 \text{ mm}$   
 overall depth  $(d + 2e)$   
 $= 185.4 + (2 \times 25)$   
 $= 235.4 \text{ mm say } 240 \text{ mm}$

The thickness is same as end batten thickness i.e. 8mm ✓  
 Hence provide 240mm wide, 260mm overall depth and 8mm thick intermediate battens.

as per cl. 7.7.2 Design of Battens

transverse SF ( $V_b$ ) = 2.5% of the total axial force  
 $= \frac{2.5}{100} \times 1100$

$\Rightarrow V_b = 27.5 \text{ kN}$   
 $= \frac{27.5 \times 10^3 \times 1300}{2 \times (55 + 200 + 55)} = 57.66 \times 10^3 \text{ N (or) } 57.66 \text{ kN}$

Shear  
 $V_b = \frac{V_b C}{NS}$

(see fig-11/51)

Moment,  $M = \frac{V_b C}{2N}$

$= \frac{27.5 \times 10^3 \times 1300}{2 \times 2} = 8.9375 \times 10^6 \text{ Nmm}$


check for stresses:

i) For End battens, shear stress  $= \frac{V_b}{\text{cls area}}$   
 $= \frac{57.66 \times 10^3}{320 \times 8}$   
 $= 22.39 \text{ N/mm}^2 < \frac{f_y}{\gamma_m} \text{ (or) } \frac{f_d}{\gamma_m}$   
 $( < 131.21 \text{ N/mm}^2 )$   
 Hence safe

Bending stress  $= \frac{M}{Z}$

$= \frac{8.9375 \times 10^6}{\left( \frac{8 \times 320^3}{6} \right)}$

$= 65.46 \text{ N/mm}^2 < \frac{f_y}{\gamma_m} < 227.27 \text{ N/mm}^2$

$z = \frac{1}{6} \times \frac{bd^3}{12} = \frac{bd^3}{6}$   


ii) For Intermediate battens,

shear stress  $= \frac{V_b}{\text{cls area}} = \frac{57.66 \times 10^3}{260 \times 8} = 27.72 \text{ N/mm}^2 < \frac{f_y}{\gamma_m} < 131.21 \text{ N/mm}^2$

Bending stress  $= \frac{M}{Z} = \frac{8.937 \times 10^6}{\left( \frac{8 \times 260^3}{6} \right)} = 99.1 \text{ N/mm}^2 < \frac{f_d}{\gamma_m} < 227.27 \text{ N/mm}^2$



connections. The connections should be designed to transmit bolts

Shear and BM.

07/3/15 using 20 mm dia. bolts strength of bolt in shear }  $V_{dsf} = \frac{f_u}{\sqrt{3}} \gamma_{mb} (n A_{nb} + n_s A_{sb})$

$$= \frac{400}{\sqrt{3} \times 1.25} (0.78 \times \frac{\pi}{4} \times 20^2)$$

In bearing,  $V_{dpb} = 2.5 k_b d t \frac{f_u}{\gamma_{mb}} = 45.27 \text{ kN}$

$e \leq 1.5 d_h$

$\leq 1.5 \times 22$

$\leq 33 \text{ mm say } 40 \text{ mm}$

$p \leq 2.5 d$

$\leq 50 \text{ mm say}$

$= 2.5 \times 0.507 \times 20 \times 8 \times \frac{410}{1.25}$

$= 66.52 \text{ kN}$

$k_b = \frac{e}{3d_o}, \frac{p}{3d_o} - 0.25, \frac{f_{ub}}{f_u}, 1.0$   
 $= 0.606, 0.507, 0.97, 1.0$

$\therefore \text{Strength of bolt} = 45.27 \text{ kN}$

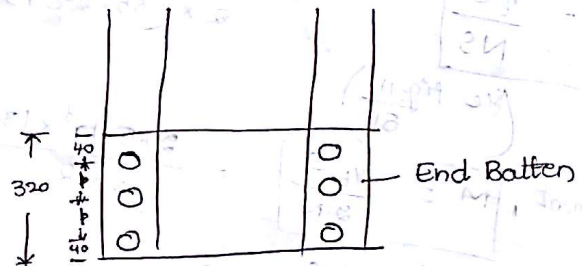
$V_b = 57.66 \text{ kN}$

$\Rightarrow$  no. of bolts required  $= \frac{57.66}{45.27} = 1.274$  Say 3 bolts i.e. to accommodate for BM also.

Each pitch  $= \frac{320 - 2 \times 40}{2}$

$\Rightarrow p = 120 \text{ mm}$

Shear to be resisted by each bolt  $= \frac{57.66}{3} = 19.22 \text{ kN}$



BM to be resisted Force in each bolt is due to shear  $= 19.22 \text{ kN}$

is due to BM  $= \frac{M x}{I x^2}$  where  $x$  is pitch

$= \frac{8.9375 \times 10^6 \times 120}{120^2 + 120^2}$

$= 37.24 \text{ kN}$

Resultant force on each bolt  $= \sqrt{19.22^2 + 37.24^2}$

$= 41.9 \text{ kN} < \text{strength of bolt } (45.27 \text{ kN})$

Hence safe

No. of batten plates required on each phase  $= \frac{\text{length of column}}{\text{batten spacing}} + 1$

$= \frac{9000}{1200} + 1$

$= 7.92$  Say 8 battens

Revised the centre to centre distance of battens  $= \frac{9 \times 10^3}{8-1} = 1285.7$

⑦

$< 1305$

Provide 2 End Barriers & 6 Intermediate barriers on each face of the column and connect it with 3 # 20 dia. bolts with an edge distance of 40 mm & a pitch of 120 mm.

chromosomes of the gametes to be lost. - not suitable for - tightly packed chromosomes for 10 months  
- the best time when the gametes are in the cell is the best time for the gametes to be lost. - not suitable for - tightly packed chromosomes for 10 months  
- the best time when the gametes are in the cell is the best time for the gametes to be lost. - not suitable for - tightly packed chromosomes for 10 months

width of breast plate is normally kept equal to that of base plate.

Concrete pedestal of size of  $24 \times 24 \times 200$  mm  
is casted connection to column base plate. Also top of  
foundation plate is welded connection to column base  
an axial fixed end of column base is used for the  
Design a slab base for a column  $250 \times 250$  mm

$\left( \frac{1 - \cos \theta}{2} \right)$

*[Faint handwritten notes and a sketch of a horizontal line with vertical tick marks below it.]*